

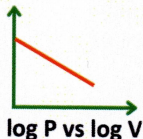
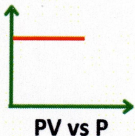
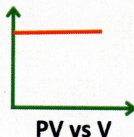
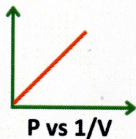
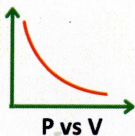
# STATES OF MATTER

## BOYLE'S LAW

$$P \propto \frac{1}{V}$$

$$PV = k_1$$

$$P_1 V_1 = P_2 V_2$$



**Graphical View**

## CHARLES LAW

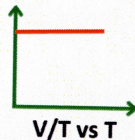
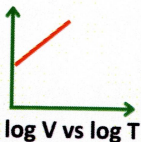
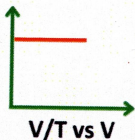
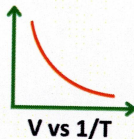
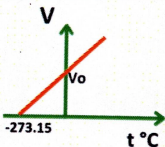
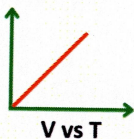
$$V \propto T$$

$$\frac{V_1}{T_1} = \frac{V_2}{T_2}$$

$$V_t = V_o + \frac{t^{\circ}C}{273.15} V_o$$



## Graphical View



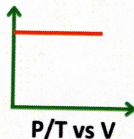
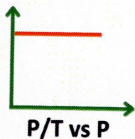
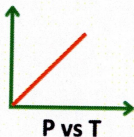
## GAY LUSSAC'S LAW

The pressure of a gas increases as its temperature increases, assuming constant mass and volume.

$$P \propto T$$

$$\frac{P_1}{T_1} = \frac{P_2}{T_2}$$

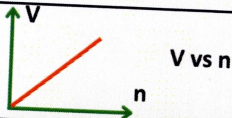
$$P = k_3 T$$



## Avogadro's law

Equal volumes of all gases under the same condition of temp and pressure contain equal no of molecules.

$$V \propto n \text{ or } \frac{V_1}{n_1} = \frac{V_2}{n_2}$$



## Ideal Gas Equation

From all the laws mentioned above

$$PV = nRT$$

where, R is a gas constant with the following values.

$$8.314 \text{ J mol}^{-1} \text{ K}^{-1}$$

$$0.0821 \text{ L atm mol}^{-1} \text{ K}^{-1}$$

$$1.98 \text{ cal mol}^{-1} \text{ K}^{-1}$$

use (25/3)

use (1/12)

use (2)

Relation of P with density

$$PM = dRT$$

- No gas is perfectly Ideal.
- Ideal nature is achieved at **High Temp, Low Pressure**

## Combined gas laws

For a fixed amount of a gas, if T, P and V changes from initial values P<sub>1</sub>, V<sub>1</sub>, T<sub>1</sub> to Final P<sub>2</sub>, V<sub>2</sub>, T<sub>2</sub>.

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$



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## Graham's Law of Diffusion

- Rate of diffusion is number of moles of gas diffused per unit time.  $r = V/T = n/T$
- The rate of diffusion or effusion of a gas is inversely proportional to the square root of its molar mass.

$$r_1 = \frac{1}{\sqrt{M_1}}$$

$$\frac{r_1}{r_2} = \sqrt{\frac{M_2}{M_1}}$$



- Volume Flow rate

$$\frac{V_1}{V_2} \times \frac{t_2}{t_1} = \sqrt{\frac{M_2}{M_1}}$$

- Moles flow rate

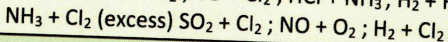
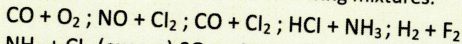
$$\frac{n_1}{n_2} \times \frac{t_2}{t_1} = \sqrt{\frac{M_2}{M_1}}$$

## Dalton's law of partial pressure

- According to this law, the total pressure of a mixture of non-reacting gas is equal to the sum of partial pressure of each gas.
- Applicable for the mixture of non reacting gases.
- For a mixture of 3 gases A, B, C

$$P_T = P_A + P_B + P_C \text{ and } P_A = x_A \cdot P_T$$

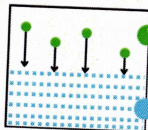
- The law is not valid for the following mixtures.





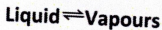
## Vapour Pressure

- The pressure exerted by vapours over the surface of liquid when liquid and vapours are in equilibrium.



Vapours

Liquid



Rate of Vaporisation =  
Rate of Condensation

### Factors Affecting Vapour Pressure

- Temperature  
 $VP \propto T$

- Intermolecular forces  
 $VP \propto 1/\text{IMF}$

$$P_{\text{moist gas}} = P_{\text{dry gas}} + VP_{\text{H}_2\text{O}} \text{ (aq. Tension)}$$

### Kinetic Theory of gases

- NO force of attraction b/w gas molecules.
- Volume of gas molecule is negligible
- Motion is straight line and random (chaotic motions)
- Collision is perfectly elastic.
- Avg.  $KE \propto \text{Absolute } T$

### Kinetic Gas Equation

$$PV = \frac{1}{3}mNV^2_{\text{rms}}$$

- P in Pa
- Volume in  $\text{m}^3$
- Mass in kg
- No. of molecules (N)
- Root mean square velocity (m/s)



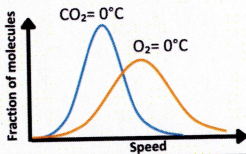
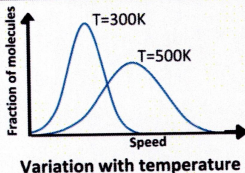
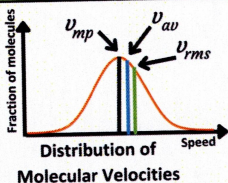
## Average Kinetic Energy

$$\text{K.E.} = \frac{3}{2}RT = \frac{3}{2}k_bT$$

Per Mole      Per molecule



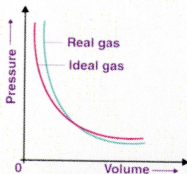
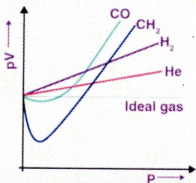
## Maxwell Boltzmann distribution of speeds



$$f(v) = 4\pi \left( \frac{m}{2\pi kT} \right)^{\frac{3}{2}} v^2 e^{-\frac{mv^2}{2kT}}$$

RMS	Average	Most probable
$v_{rms} = \sqrt{\frac{3RT}{M}}$	$v_{av} = \sqrt{\frac{8RT}{\pi M}}$	$v_{mp} = \sqrt{\frac{2RT}{M}}$
Relation ( $v_{mp} : v_{av} : v_{rms}$ ) = 1 : 1.128 : 1.224		





## Deviation from Ideal Behaviour

- Pressure Correction

$$P_{\text{ideal}} = P_{\text{real}} + \frac{an^2}{V^2}$$

- Volume Correction

$$V_{\text{ideal}} = V_{\text{container}} - nb$$

## Equation of State

$$\left(p + \frac{n^2 a}{V^2}\right)(V - nb) = nRT$$

**a** = Force of attraction measure  
( $\text{atm L}^2 \text{mol}^{-2}$ )

**b** = Excluded volume ( $\text{L mol}^{-1}$ )

## Compressibility factor, Z

$$Z = \frac{V_{\text{real}}}{V_{\text{ideal}}} = \frac{PV_{\text{real}}}{RT}$$

Z is a factor to check the deviation of real gas from ideality

**For Attraction**

$$V_{\text{real}} < V_{\text{ideal}} \Rightarrow Z < 1$$

**For Repulsion**

$$V_{\text{real}} > V_{\text{ideal}} \Rightarrow Z > 1$$

**Boyles temperature**

T at which Ideal = Real

$$T_b = a/Rb$$

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## Collision Parameters

**Mean Free Path**

**Average time between collisions**

$$\lambda \propto \frac{T}{P}$$

$$\lambda = \frac{1}{\sqrt{2}\pi\sigma^2 N^*}$$

$\sigma$  = Collision diameter  
 $N^*$  = Number Density

**Collision Frequency**

$$z = \sqrt{2}\pi\sigma^2 V_{avg} N^*$$

## Liquefaction of gases

**Critical Temperature**

$$T_c = \frac{8a}{27Rb}$$

**Critical Volume**

$$V_c = 3b$$

**Critical Pressure**

$$P_c = \frac{a}{27b^2}$$

**Comp. Factor ( $Z_c$ )**

$$\frac{P_c V_c}{RT_c} = \frac{3}{8} < 1$$

## Condition for Liquefaction

- Liquefaction  $\propto a/b$  (Vander waals constants)
- $\text{He} < \text{H}_2 < \text{N}_2 < \text{O}_2 < \text{CO}_2 < \text{NH}_3 < \text{H}_2\text{O}$  (For Liquefaction)

